

RP-18-19



# REVIEW OF RESEARCH

IMPACT FACTOR : 5.7631 (UIF)

ISSN: 2249-894X

VOLUME - 1 | ISSUE - 2 | MARCH - 2019

## VARIATION OF DAMPING LENGTH AND WAVELENGTH IN NORTH POLAR CORONAL HOLES OF SOLAR ATMOSPHERE

Bhagvat K. Kumthekar

Department of Physics, NutanMahavidyalaya, SailuDistParbhani -431 503 (MS) India

Email: bkumthekar@gmail.com

### ABSTRACT :

In the present paper, I would like to discuss about variation of damping length and wavelength in the region of  $1.05R_{\odot}$  to  $1.35R_{\odot}$  and in different cases like (i) Magnetic diffusivity only (ii) viscosity only and (iii) when both are present. It shows that Comparison of the fast and slow modes explicitly shows that the damping length as well as the wavelength for the fast-mode waves is much larger than those for the slow-mode waves.

### INTRODUCTION:

The role of magnetohydrodynamics (MHD) waves has been discussed extensively in solar physics for understanding the outstanding problems of solar coronal heating and the solar wind acceleration Mechanisms [1]. For derivation of dispersion relation we have to consider following MHD equation

$$\rho \frac{\partial v}{\partial t} + \rho(v \cdot \nabla)v = \frac{1}{\mu} (\nabla \times B) \times B + \rho \nu \nabla^2 V \quad (1)$$

$$\frac{\partial B}{\partial t} = \nabla \times (v \times B) + \eta \nabla^2 B \quad (2)$$

$$\nabla \cdot B = 0 \quad (3)$$

The equations (1), (2) and (3) are known as momentum equation, Induction equation and Magnetic flux conservation equation respectively. Where  $v$  is the velocity,  $B$  the magnetic field and  $\rho, \mu, \eta, \nu$  are, respectively, the mass density, Magnetic permeability, magnetic diffusivity and the coefficient of viscosity.

Taking the perturbations from the equilibrium (Priest [2]) and linearize the equations (1) through (3) by neglecting squares and products of the small quantities. After solving above equations we get a dispersion relation as follows

$$\omega^2 = k^2 [v_A^2 - i\omega(\nu + \eta)] + \nu \eta k^4 \quad (4)$$

Where  $V_A = B_0 / (\sqrt{\mu \rho_0})$  is the Alfvén velocity. The dispersion relation was obtained by Pekunu et al. [3] & Kumthekar [4]. This dispersion relation is applied for the plasma in the North Polar Coronal Hole where assumed the angular frequency  $\omega$  to be a real quantity and the wave number  $k$  as a complex quantity.

### RESULT AND DISCUSSION:

For a given value of  $\omega = 2\pi/\tau$  and the physical parameters discussed in the Kumthekar [3] and solved with the help of a FORTRAN program. I assumed the angular frequency  $\omega$  to be a real quantity and the wave

PRINCIPAL

Nutan Mahavidyalaya  
SELU, Dist. Parbhani



number  $k$  as a complex quantity so that  $k = kr + iki$ . When both the  $kr$  and  $ki$  are positive numbers, they are related to the damping length  $D$  and the wavelength  $\lambda$  of the wave as Chandra et al. [5]

$$D = \frac{2\pi}{k_i} \quad \text{and} \quad \lambda = \frac{2\pi}{k_r}$$

Equation (4) is a simple quadratic equation it can be solved for getting roots of equation. This equation can be studied for three cases (i) Magnetic diffusivity only (ii) viscosity only and (iii) when both are present.

**Case I: Magnetic diffusivity:**

Let us consider the case of magnetic diffusivity only. That is, there is no viscosity ( $\nu = 0$ ). For this case, equation (4) gives  $kr$  and  $ki$  values. Then we can apply a condition  $\omega \ll v_A^2$ , we get

$$k_r = \frac{\omega}{v_A} \quad \text{and} \quad k_i = \frac{\omega^2}{2v_A^3}$$

Thus, we have two roots; one with positive values of  $kr$  and  $ki$ , and the other with the negative values. For the positive values, the damping length  $D$  and wavelength  $\lambda$  are calculate as a function of  $R$ , for  $\tau = 10^{-2}$  s,  $10^{-3}$  s and  $10^{-4}$  s and are given in Fig.1 (a). As from the expressions, here the damping length is much larger than the wavelength. While  $D$  shows a large variation, with a maximum around  $1.2R \odot$ , the  $\lambda$  remains nearly constant. Fig.1 (a) shows that the wavelength is proportional to  $\tau$  whereas the damping length is proportional to  $\tau^2$ .

**Case II: Viscosity only:**

Let us consider the case of viscosity only. That is, there is no magnetic diffusivity ( $\eta = 0$ ). For this case, equation (4) gives  $kr$  and  $ki$  values. Then we can apply a condition  $\omega \nu \gg v_A^2$ , we get

$$k_r = \frac{\sqrt{\omega}}{\sqrt{2\nu}} \quad \text{and} \quad k_i = \frac{\sqrt{\omega}}{\sqrt{2\nu}}$$

Again, we have two roots; one with positive values of  $kr$  and  $ki$ , and the other with the negative values. For the positive values, the damping length  $D$  and wavelength  $\lambda$  are calculate as a function of  $R$ , for  $\tau = 10^{-2}$  s,  $10^{-3}$  s and  $10^{-4}$  s and are given in Fig.1 (b).

As from the expressions, as long as  $\omega \nu \gg v_A^2$ , the damping length and the wavelength are equal to each other. There is a maximum around  $1.2R \odot$ . It is the case for  $\tau = 10^{-3}$  s and  $10^{-4}$  s. But, for  $\tau = 10^{-2}$  s, the  $D$  and  $\lambda$  differ slightly from each other, showing that the condition  $\omega \nu \gg v_A^2$  is not satisfied here. There is a maximum around  $1.2R \odot$ .

**Case III: Both are Present  $\nu \neq 0$  and  $\eta \neq 0$ .**

Equation (4) is a quadratic equation in  $k^2$  and therefore, its roots are of the form of two pairs:  $\pm(kr1 + iki1)$  and  $\pm(kr2 + iki2)$ . These two pairs for the roots correspond to the fast-mode and slow-mode waves. The damping length  $D$  and wavelength  $\lambda$  for the two modes as a function of  $R$  for  $\tau = 10^{-2}$  s,  $10^{-3}$  s and  $10^{-4}$  s are shown in Fig. 2. It is interesting to note that the variation of  $D$  and  $\lambda$  for the fast-mode wave is similar to that for the case of  $\eta = 0$ . The slow-mode wave shows an opposite behaviour for the variation of  $D$  as well as  $\lambda$ . There is a minimum around  $1.2R \odot$ . Here, also,  $D$  is nearly equal to  $\lambda$  for  $\tau = 10^{-3}$  s and  $10^{-4}$  s. But, for  $\tau = 10^{-2}$  s, the  $D$  and  $\lambda$  differ slightly from each other. Comparison of the fast and slow modes explicitly shows that the damping length as well as the wavelength for the fast-mode waves is much larger than those for the slow-mode wave. Thus, the slow-mode waves cannot propagate through the corona.

*[Signature]*  
**PRINCIPAL**  
 Nutan Mahavidyalaya  
 SELU, Dist. Parbhani



**ACKNOWLEDGMENTS**

I am heartily thankful to Prof. Suresh Chandra for his valuable guidance for this paper and my research carrier. Also Dr. S. S. Kulkarni, Principal, NutanMahavidyalaya, SeluDistParbhanifor providing necessary facilities and encouragement is thankfully acknowledged. A part of this work was done during our visit to IUCAA, Pune. I acknowledge the support from the IUCAA, Pune.

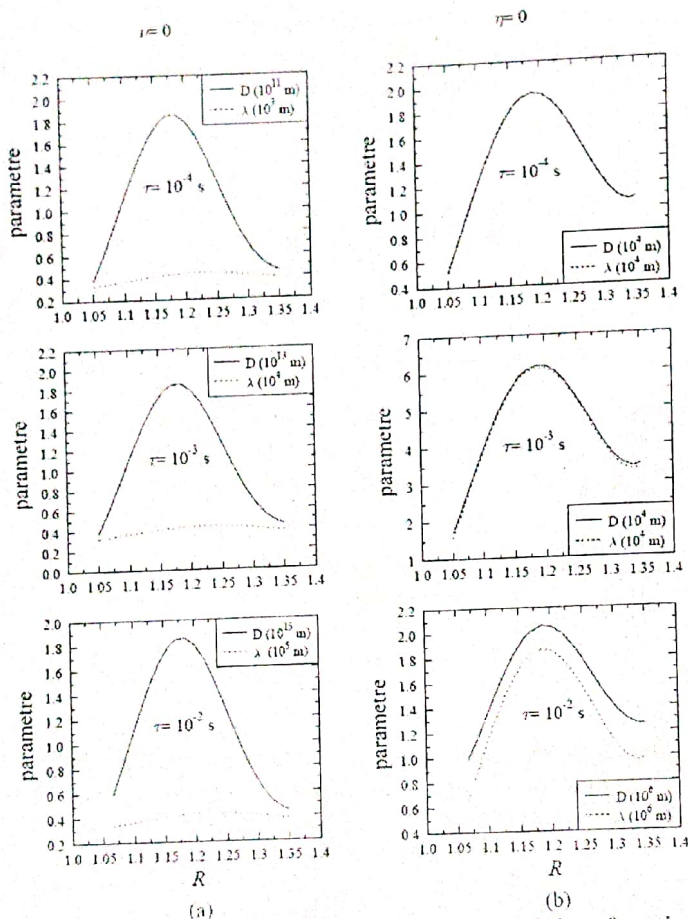


Fig. 1: Variation of damping length  $D$  and the wavelength  $\lambda$  as function of  $R$  for  $\tau = 10^{-2}$  s,  $10^{-3}$  s and  $10^{-4}$  s for two cases  $\nu=0$  and  $\eta=0$ .

*[Signature]*  
**PRINCIPAL**  
 Nutan Mahavidyalaya  
 SELU, Dist. Parbhani

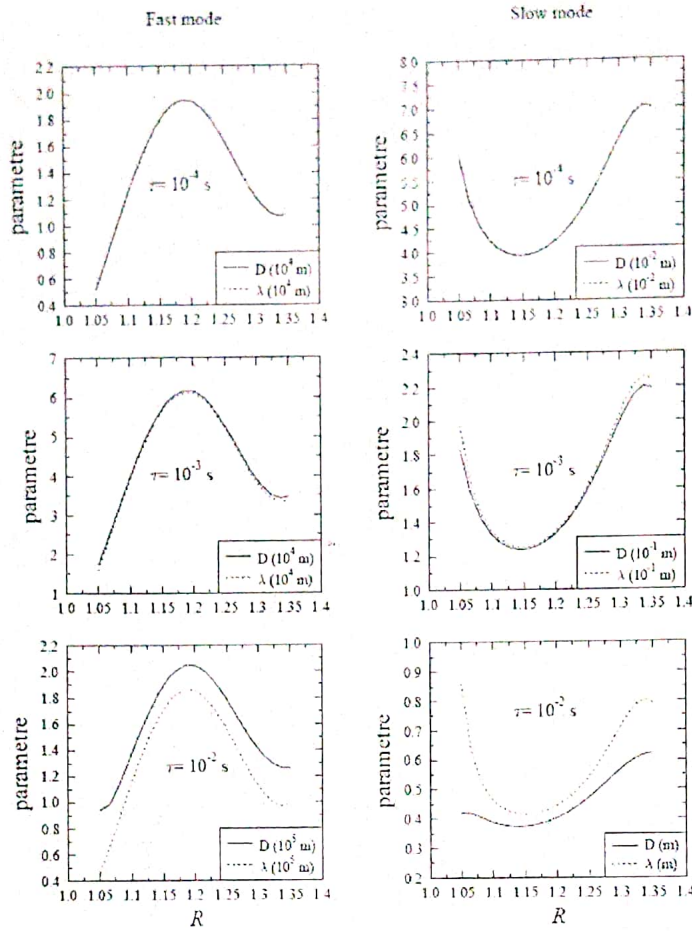



Fig. 2: Variation of damping length  $D$  and the wavelength  $\lambda$  for fast mode and slow mode waves as function of  $R$  for  $\tau = 10^{-2}$  s,  $10^{-3}$  s and  $10^{-4}$  s for two cases  $v \neq 0$  and  $\eta \neq 0$ .

REFERENCES:

- [1] E N Parker *Space Sci Rev*, 4, 666 (1965)
- [2] E R Priest *Solar Magnetohydrodynamics*. (Dordrecht, Holland: D. Reidel Publishing Company) (1982)
- [3] E R Pekunlu, Z Bozkurt, M Afsar, E Soydugan and F Soydugan *Mon Notices Roy Astron Soc*, 336, 1195 (2002)
- [4] B. K. Kumthekar, *International Journal of Innovative Science, Engineering & Technology*, (IJSET) Vol. 4 Issue 6, (2017)
- [5] Chandra S, B. K. Kumthekar & G. M. Dak, *Indian Journal of Radio & Space Physics (IJRSP)* 39, (2010)

  
**PRINCIPAL**  
**Nutan Mahavidyalaya**  
**SELU, Dist. Parbhani**